

First Name: _____ Last Name: _____

15 PT.

Problem 1

Design a circuit that counts the number of 0's present in 4 inputs A, B, C and D. Its output is a multi-bit, representing that count in binary. For example, 0101 has two zeros and therefore the output should be a binary representing 2.

- Write the truth table for this circuit.
- Find the minimized logic equations in SOP and POS for each output
- Draw the corresponding all NAND and all NOR gates logic diagram for this circuit. Label all inputs and outputs.

15 PT.

Problem 2

Design a circuit with inputs A,B,C, and D. Let the two inputs AB represent a two-bit number with A as the high order bit, and CD represent another two-bit number. That is, the values on AB represent four values 00 (0), 01 (1), 10 (2), and 11 (3). The circuit has three outputs: G, E, and L. Output G, E, and L should be 1 only if the number represented by AB is greater, equal, and less than the number represented by CD, respectively.

- Write the truth table for this circuit.
- Find the minimized logic equations in SOP and POS for each output
- Draw the corresponding all NAND and all NOR gates logic diagram for this circuit. Label all inputs and outputs.

20 PT.

Problem 3

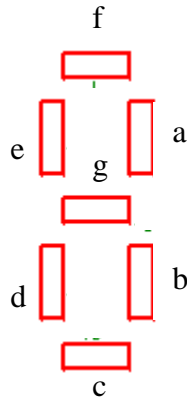
Design a circuit that can convert a 4-input BCD code into a Gray code.

- Write the truth table for this circuit.
- Find the minimized logic equations in SOP and POS for each output
- Draw the corresponding all NAND and all NOR gates logic diagram for this circuit. Label all inputs and outputs.

25 PT.

Problem 4

There is an integrated circuit called a BCD-seven segment decode that takes 4 inputs and has seven output. The inputs represent a number between 0 and 9, and each of the seven outputs corresponds to one of seven LED's in a seven-segment display. A typical seven-segment display is shown below.



- Write the truth table for each segment "a, b, c, d, e, f, g" with inputs A, B, C, and D. Make sure to adhere to the indicated segment notations.
- Simplify each output in Minimum S.O.P.
- Implement each output using all NAND gates.

15 PT.

Problem 5

Design a 1 out of 4 decoder with active low outputs and two enable lines, one active low and one active high.

15 PT.

Problem 6

Using the decoder in Problem 5, design a 1 out of 16 decoder with active low outputs.

15 PT.

Problem 7

Implement the following Boolean expression using a decoder and an OR gate – You may choose a decoder with active high or active low outputs.

$$F(A, B, C, D) = \sum m(0, 1, 2, 4, 5) + d(3, 6)$$

15 PT.

Problem 8

Implement the following Boolean expression using a decoder and a NAND gate.

$$F(X, Y, Z, W) = \prod M(0, 6, 8, 13, 14) + d(2, 4, 10)$$

15 PT.

Problem 9

Obtain the truth table for a 16×4 priority encoder with inputs $D_0 - D_{15}$, and output X, Y, Z, W, V (valid). Assume higher index has higher priority.

15 PT.
Problem 10
Design an 8×1 Mux.

15 PT.
Problem 11
Implement an 8×1 Mux using 2×1 Mux's.

15 PT.
Problem 12
Implement the following Boolean expression using an 8×1 Mux.

$$F(A, B, C, D) = \sum m(4, 6, 7, 8, 12, 15)$$

15 PT.
Problem 13
Repeat Problem 12 using a 4×1 Mux and external gates.

15 PT.
Problem 14
Implement the following functions using a PLE.

$$F_1 = \sum m(0, 2, 5, 7, 8, 10, 12, 13)$$

$$F_2 = \sum m(0, 2, 4, 5, 6, 7, 8, 10, 13, 15)$$

$$F_3 = \sum m(1, 2, 3, 5, 7, 9, 10, 11, 13, 15)$$

15 PT.
Problem 15
Repeat problem 14 for a PAL. (You must simplify your answer)

15 PT.
Problem 16
Repeat problem 14 for a PLA. (You must simplify your answer)
Note: you may download blank PLD sheets from http://www.engr.newpaltz.edu/~bai/EGC220/PLD_symbol.pdf and mark programmable cell with \times and fixed cell with \blacksquare .

1/2

A	B	C	D	X	Y	Z
0	0	0	0	1	0	0
0	0	0	1	0	1	1
0	0	1	0	0	1	1
0	0	1	1	0	1	0
0	1	0	0	0	1	1
0	1	0	1	0	1	0
0	1	1	0	0	1	0
0	1	1	1	0	0	1
1	0	0	0	0	1	1
1	0	0	1	0	1	0
1	0	1	0	0	1	0
1	0	1	1	0	0	1
1	1	0	0	0	1	0
1	1	0	1	0	0	1
1	1	1	0	0	0	1
1	1	1	1	0	0	0

1	0	0	0
0	0	0	0
0	0	0	0
0	0	0	0

$$X = \bar{A}\bar{B}\bar{C}\bar{D}$$

		\bar{C}	C	
	\bar{A}	\bar{B}	B	
\bar{A}	0	1	1	1
A	1	1	0	1
A	1	0	0	0
A	1	1	0	1
	\bar{D}	D	\bar{D}	

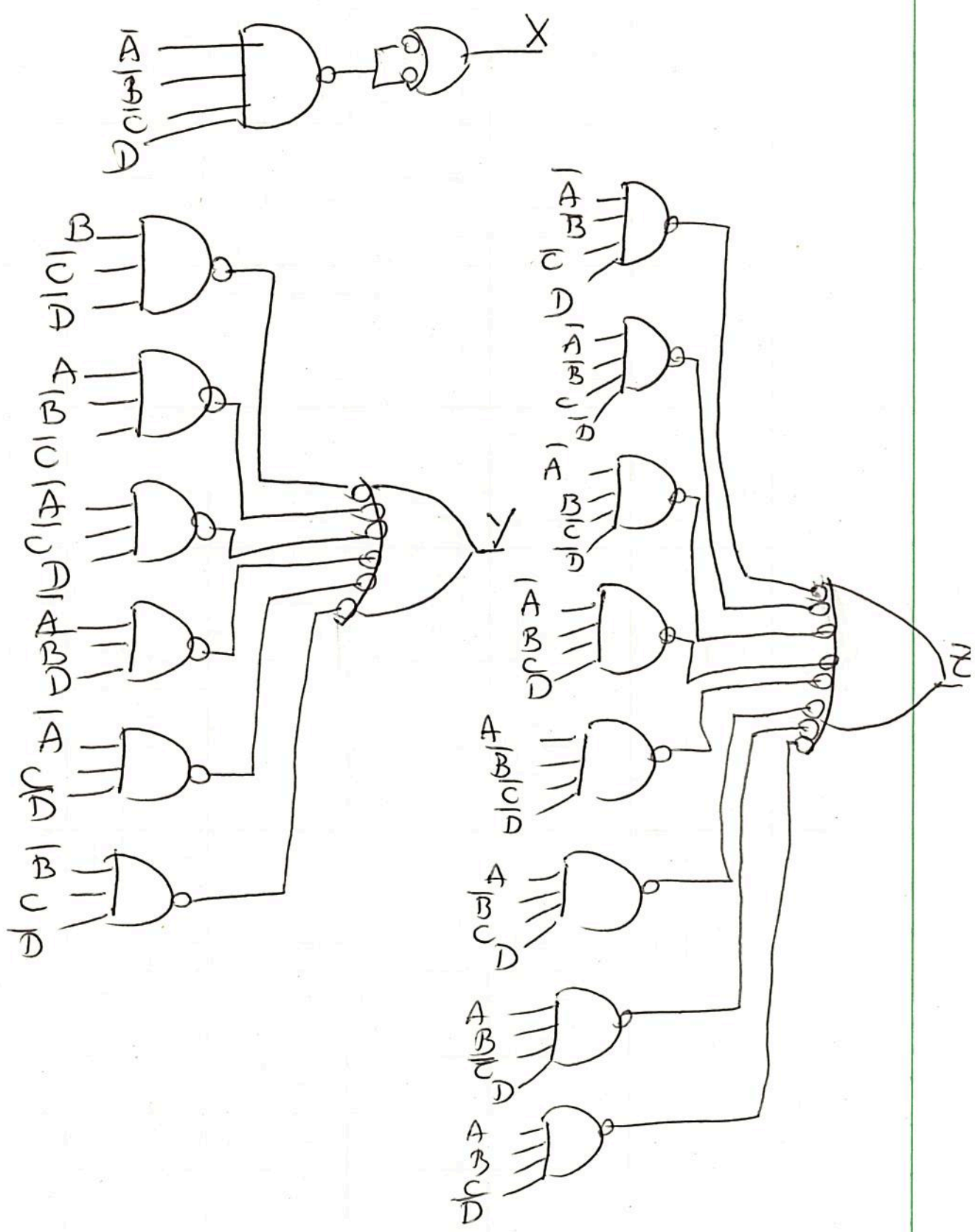
$$Y = \bar{B}\bar{D}\bar{C} + \bar{A}\bar{B}\bar{C} + \bar{A}\bar{C}\bar{D}$$

$$+ \bar{A}\bar{B}D + \bar{A}\bar{C}D + \bar{B}CD$$

(other options / combinations are possible)

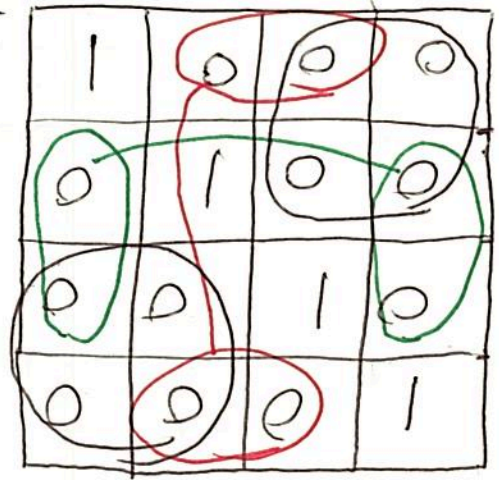
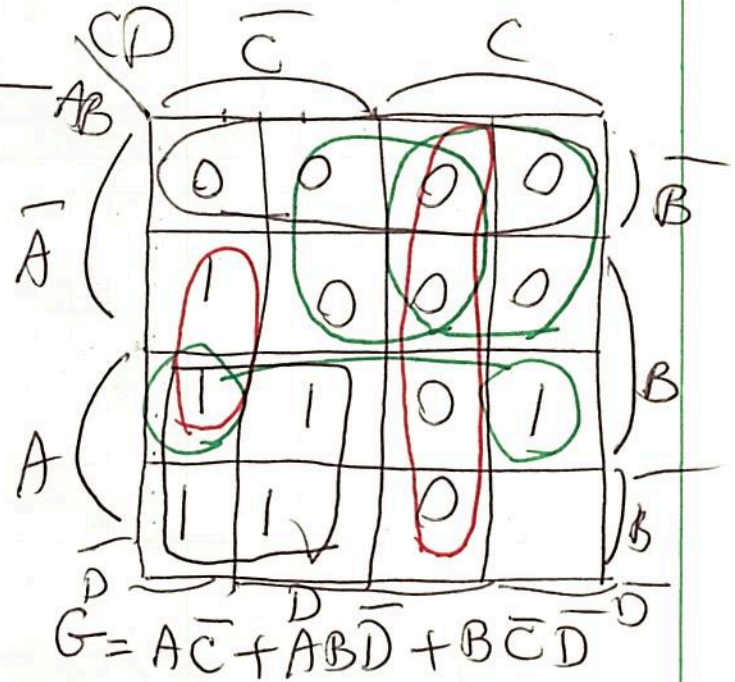
$$Z = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}BCD + A\bar{B}\bar{C}\bar{D} + A\bar{B}CD + A\bar{B}\bar{C}D + ABC\bar{D} + ABCD$$

0	1	0	1
1	0	1	0
0	1	0	1
1	0	1	0



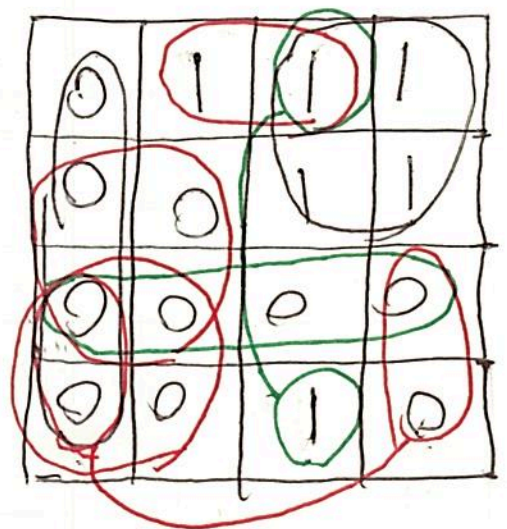
2)

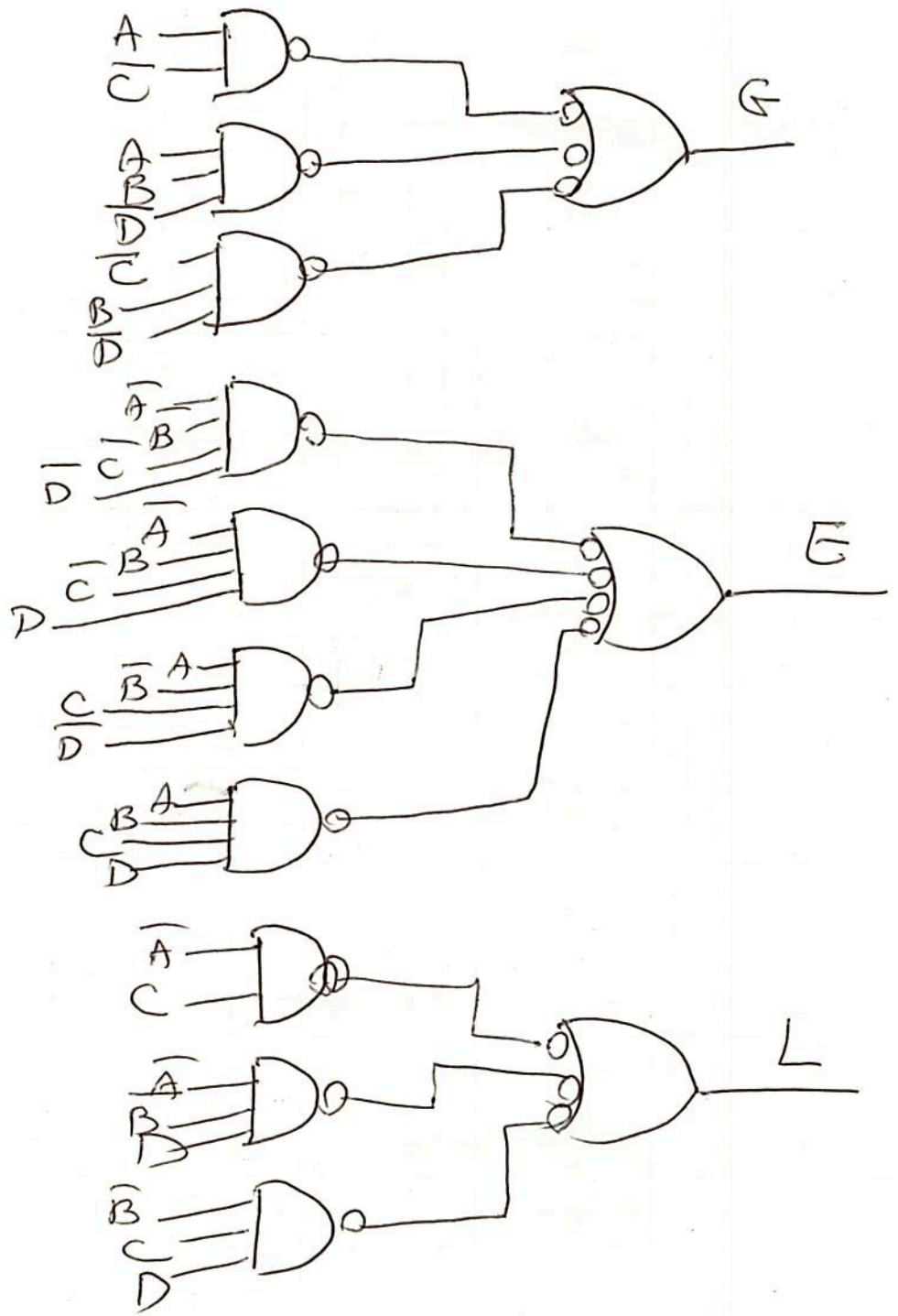
A	B	C	D	G	E	L
0	0	0	0	0	1	0
0	0	0	1	0	0	1
0	0	1	0	0	0	1
0	0	1	1	0	0	1
0	1	0	0	1	0	0
0	1	0	1	0	1	0
0	1	1	0	0	0	1
0	1	1	1	0	0	1
1	0	0	0	1	0	0
1	0	0	1	1	0	0
1	0	1	0	0	1	0
1	0	1	1	0	0	1
1	1	0	0	1	0	0
1	1	0	1	1	0	0
1	1	1	0	1	0	0
1	1	1	1	0	1	0



$E = \bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}CD$

$L = \bar{A}C + \bar{A}\bar{B}D + \bar{B}CD$





Min. P.O.S

$$\bar{G} = \bar{A}\bar{B} + \bar{A}D + \bar{A}C + CD + BC$$

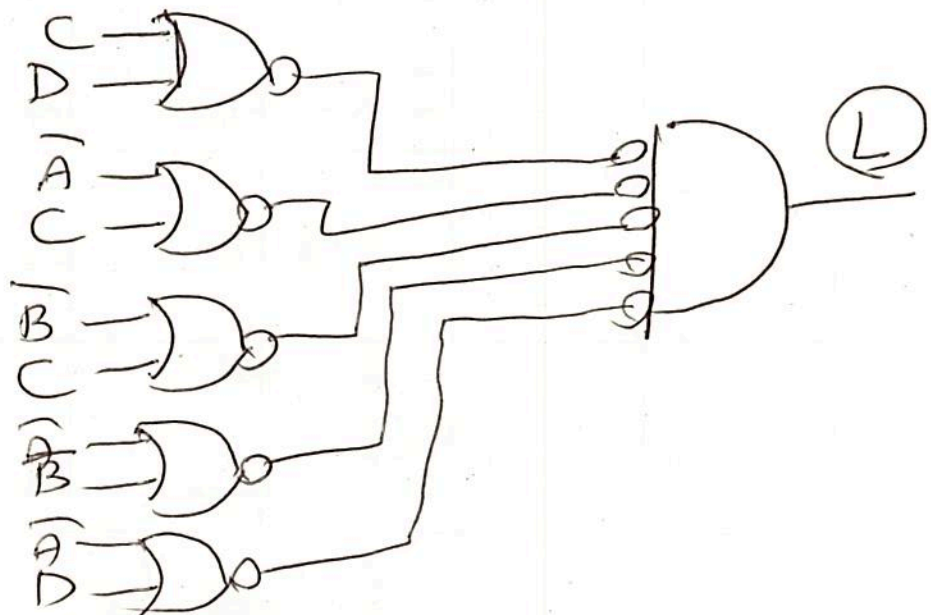
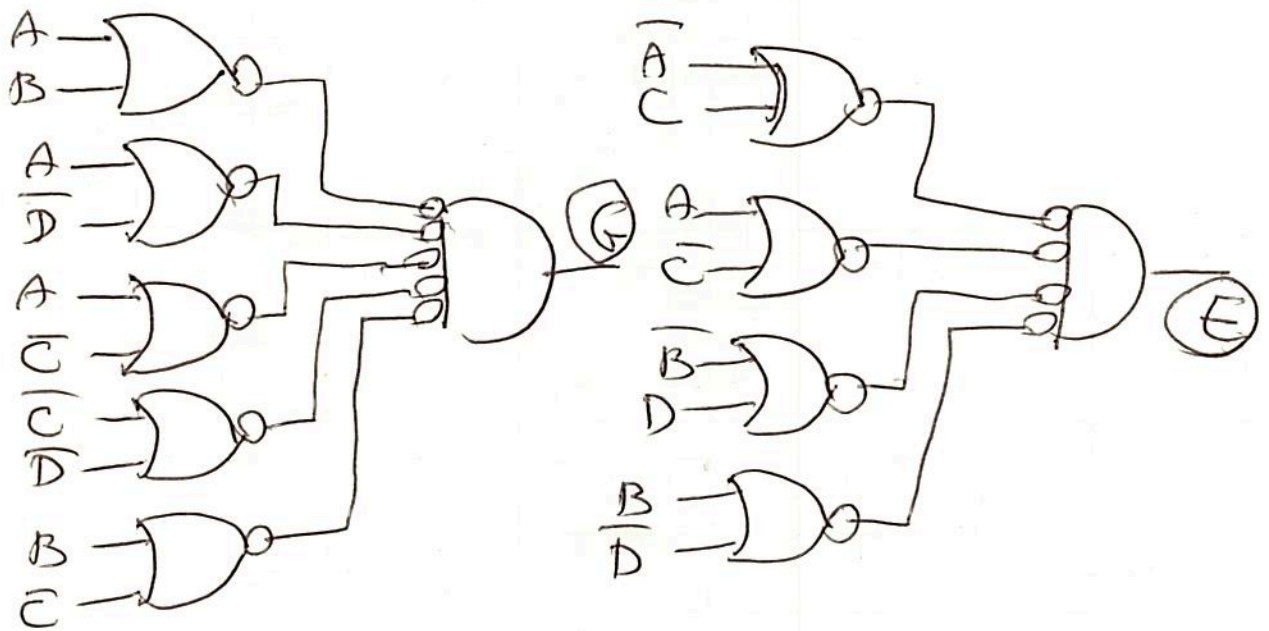
$$G = (A+B)(A+D)(A+C)(\bar{C}+\bar{D})(B+C)$$

$$\bar{E} = A\bar{C} + \bar{A}C + B\bar{D} + \bar{B}D$$

$$E = (\bar{A}+C)(A+\bar{C})(\bar{B}+D)(B+\bar{D})$$

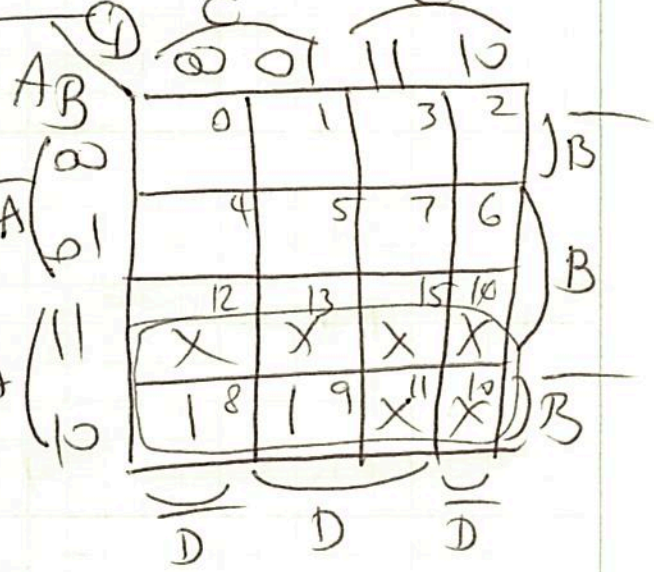
$$\bar{L} = \bar{C}\bar{D} + A\bar{C} + B\bar{C} + AB + A\bar{D}$$

$$L = (C+D)(A+C)(B+C)(\bar{A}+\bar{B})(\bar{A}+D)$$

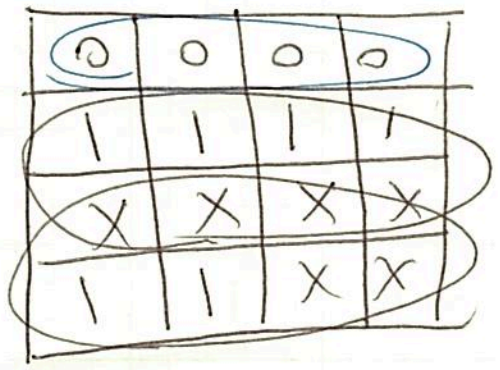


3/

A	B	C	D	G	R	a	Y
0	0	0	0	0	0	0	0
0	0	0	1	0	0	0	1
0	0	1	0	0	0	1	1
0	0	1	1	0	0	1	0
0	1	0	0	0	1	1	0
0	1	0	1	0	1	1	1
0	1	1	0	0	1	0	1
0	1	1	1	0	1	0	0
1	0	0	0	1	1	0	0
1	0	0	1	1	1	0	1
1	0	1	0	X	X	X	X
1	0	1	1	X	X	X	X
1	1	0	0	X	X	X	X
1	1	0	1	X	X	X	X
1	1	1	0	X	X	X	X
1	1	1	1	X	X	X	X

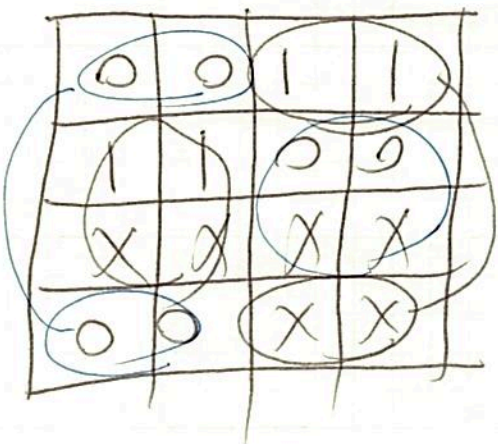


$G = A$



$R = A + B$

$R = A + B$



$a = B\bar{C} + \bar{B}C$

$\bar{a} = \bar{B}\bar{C} + BC$

$a = (B + C)(\bar{B} + \bar{C})$

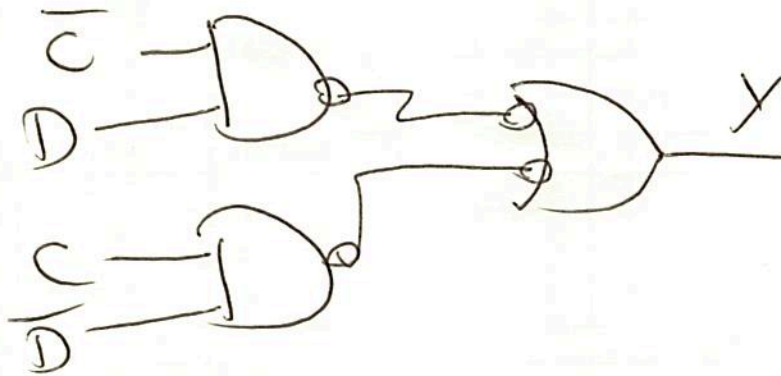
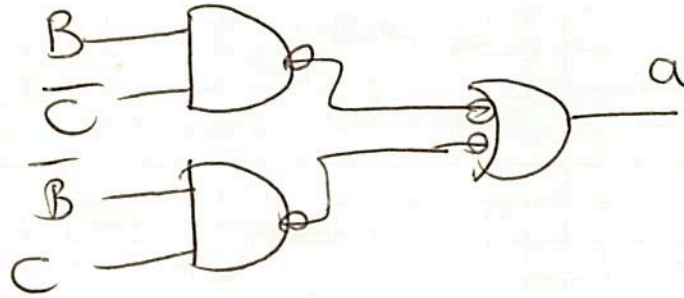
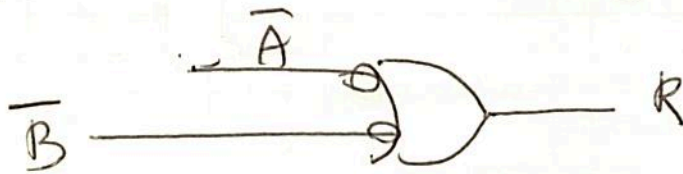


0	1	0	1
0	1	0	1
X	X	X	X
0	0	X	X

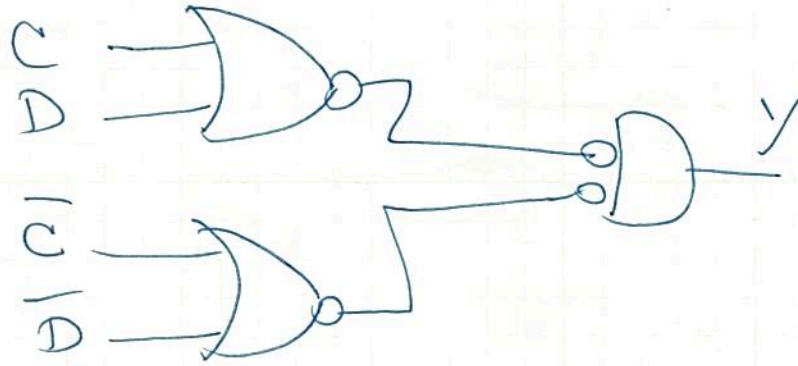
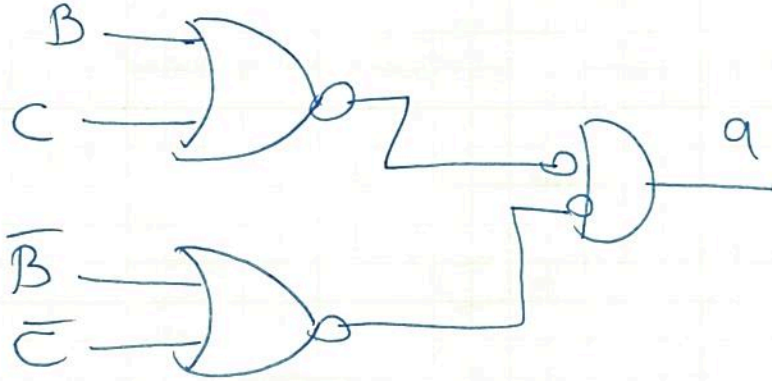
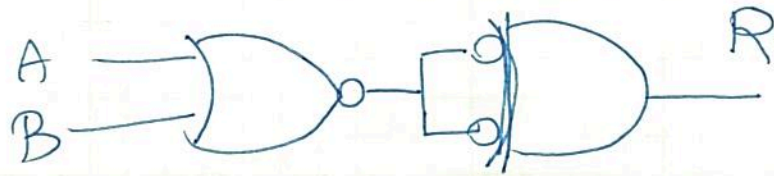
$$Y = \bar{C}D + C\bar{D}$$

$$\bar{Y} = \bar{C}\bar{D} + CD$$

$$Y = (C+D)(\bar{C}+\bar{D})$$



C./



4)

$\frac{e|g|a}{d|c|b}$

D	C	B	A	a	b	c	d	e	f	g
0	0	0	0	1	1	1	1	1	1	0
0	0	0	1	1	1	0	0	0	0	0
0	0	1	0	1	0	1	1	0	1	1
0	0	1	1	1	1	1	0	0	1	1
0	1	0	0	1	1	0	0	1	0	1
0	1	0	1	0	1	1	0	1	1	1
0	1	1	0	0	1	1	1	1	1	1
0	1	1	1	1	1	0	0	0	1	0
1	0	0	0	1	1	1	1	1	1	1
1	0	0	1	1	1	1	0	1	1	1
1	0	1	0	X	X	X	X	X	X	X
1	0	1	1	X	X	X	X	X	X	X
1	1	0	0	X	X	X	X	X	X	X
1	1	0	1	X	X	X	X	X	X	X
1	1	1	0	X	X	X	X	X	X	X
1	1	1	1	X	X	X	X	X	X	X

$\overline{A} \begin{matrix} \overline{CD} & \overline{C} & C \end{matrix}$
 $\begin{matrix} \overline{D} & D & \overline{D} \end{matrix}$
 $a = \overline{B} + \overline{C}\overline{D} + CD$
 $b = \overline{C} + D$

$$c = A + \bar{B}\bar{D} + C\bar{B} + C\bar{D} + BC\bar{D}$$

1	0	1	1
0	1	0	1
X	X	X	X
1	1	X	X

$$d = \bar{B}\bar{D} + C\bar{D}$$

1	0	0	1
0	0	0	1
X	X	X	X
1	0	X	X

$$e = A + \bar{C}\bar{D} + BC\bar{C} + B\bar{D}$$

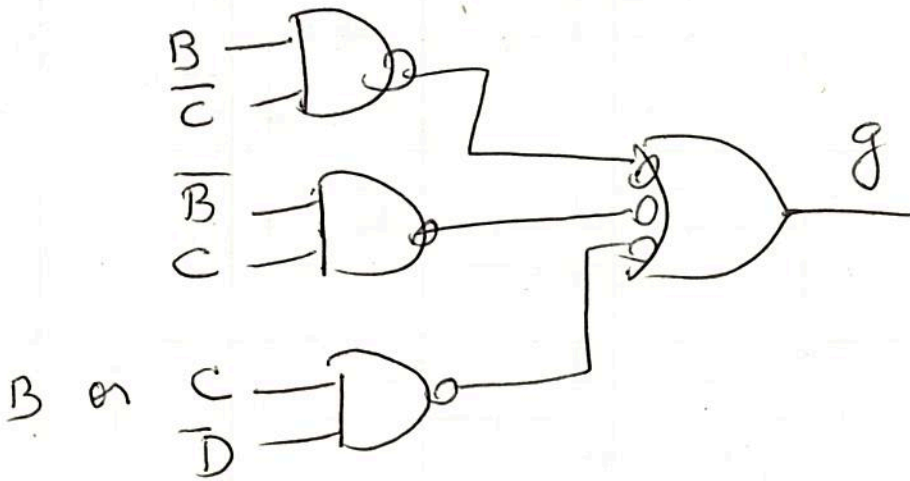
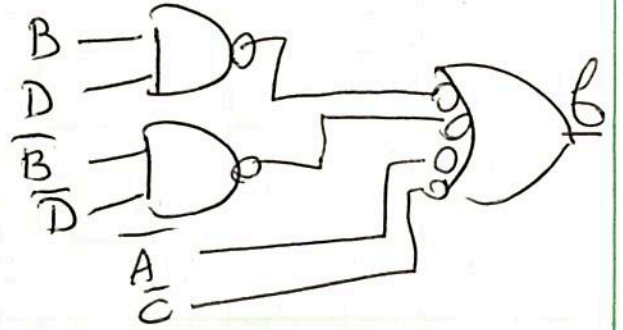
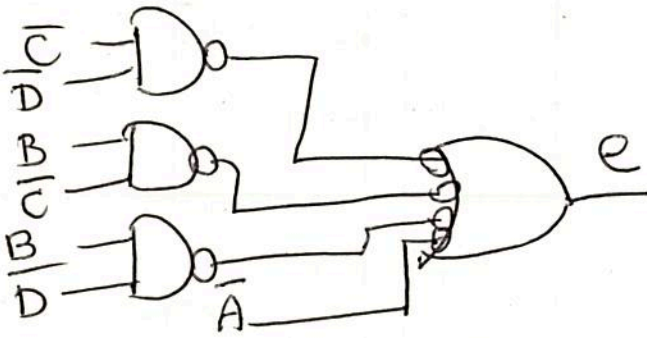
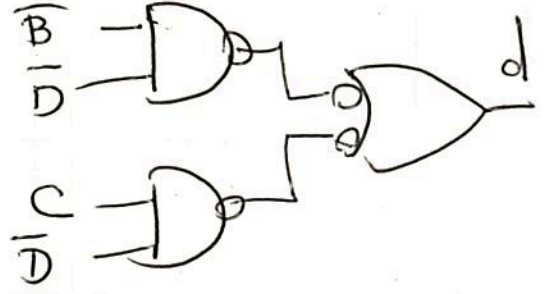
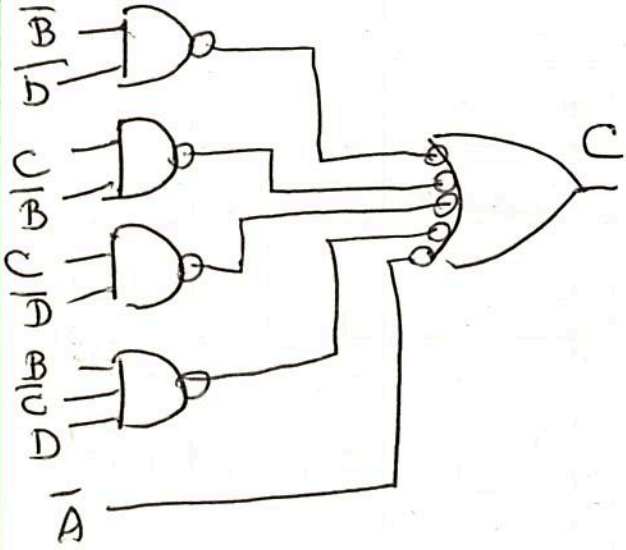
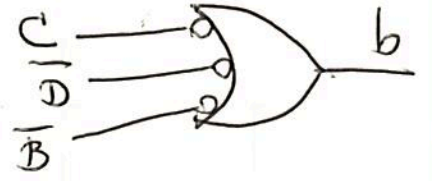
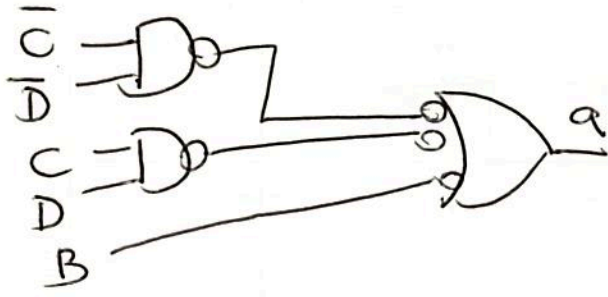
1	0	0	0
1	1	0	1
X	X	X	X
1	1	X	X

$$f = A + C + B\bar{D} + \bar{B}\bar{D}$$

1	0	1	1
0	1	1	1
X	X	X	X
1	1	X	X

0	0	1	1
1	1	0	1
X	X	X	X
1	1	X	X

$$g = A + B\bar{C} + \bar{B}C + \begin{cases} CD \\ C\bar{D} \\ B\bar{D} \end{cases}$$



5/

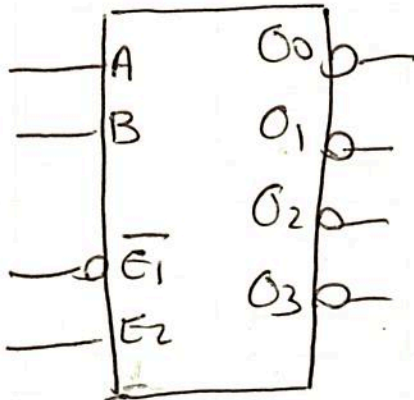
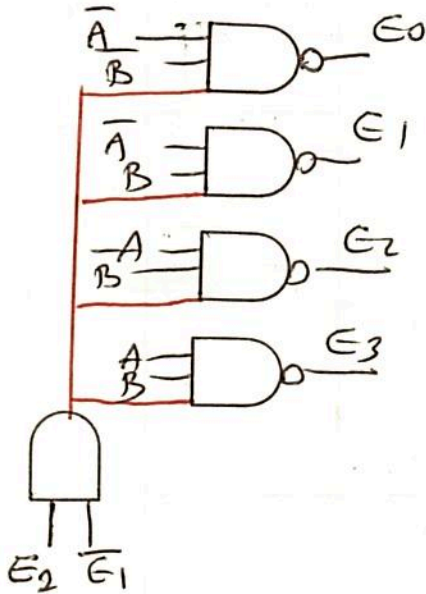
E_1	E_2	A	B	O_3	O_2	O_1	O_0
1	X	X	X	1	1	1	1
X	0	X	X	1	1	1	1
0	1	0	0	1	1	1	0
0	1	0	1	1	1	0	1
0	1	1	0	1	0	1	1
0	1	1	1	0	1	1	1

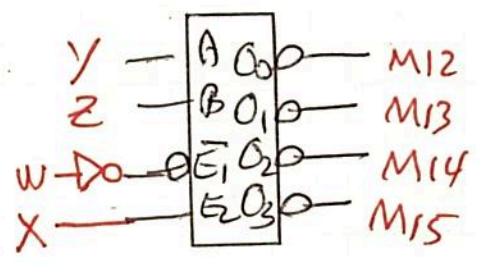
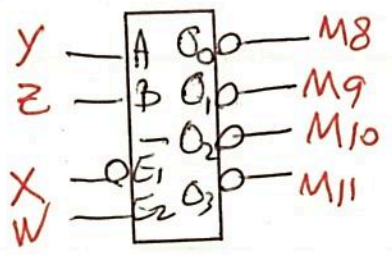
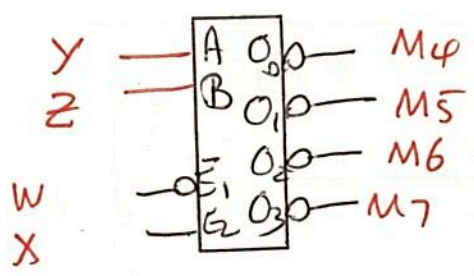
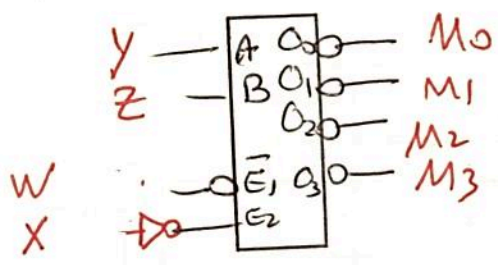
$$\overline{O_0} = \overline{E_1} E_2 \overline{A} \overline{B}$$

$$\overline{O_1} = \overline{E_1} E_2 A \overline{B}$$

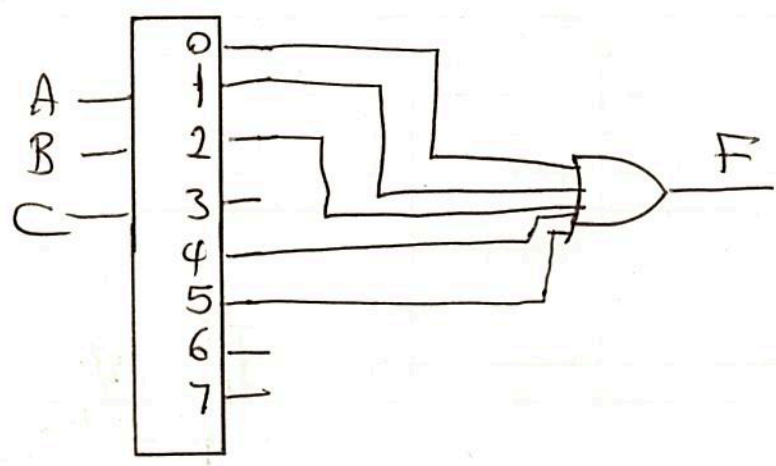
$$\overline{O_2} = \overline{E_1} E_2 A B$$

$$\overline{O_3} = \overline{E_1} E_2 \overline{A} B$$



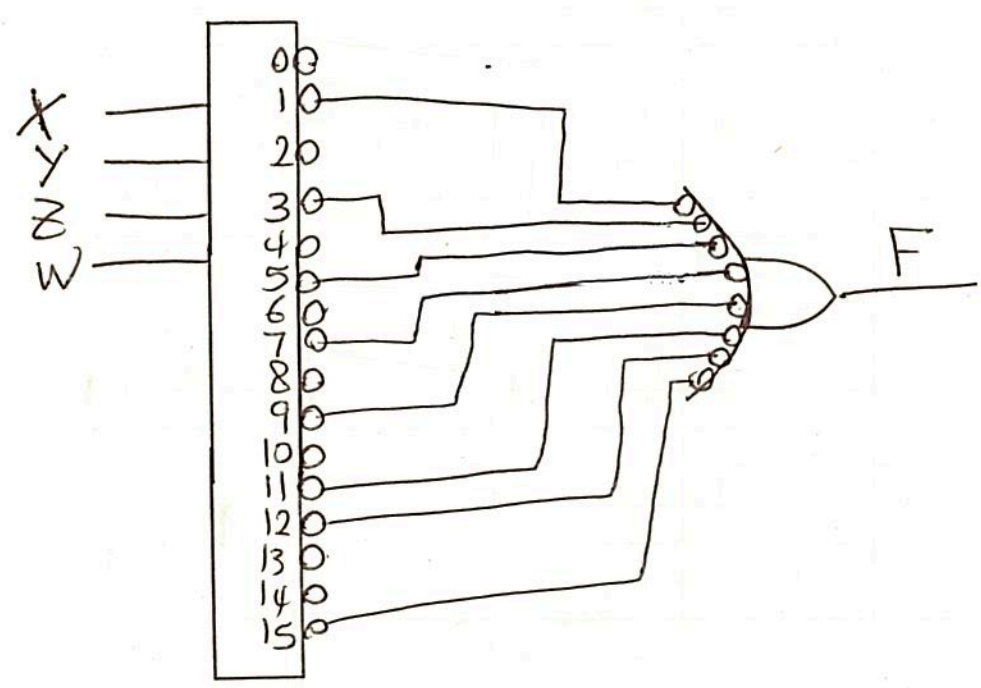


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8

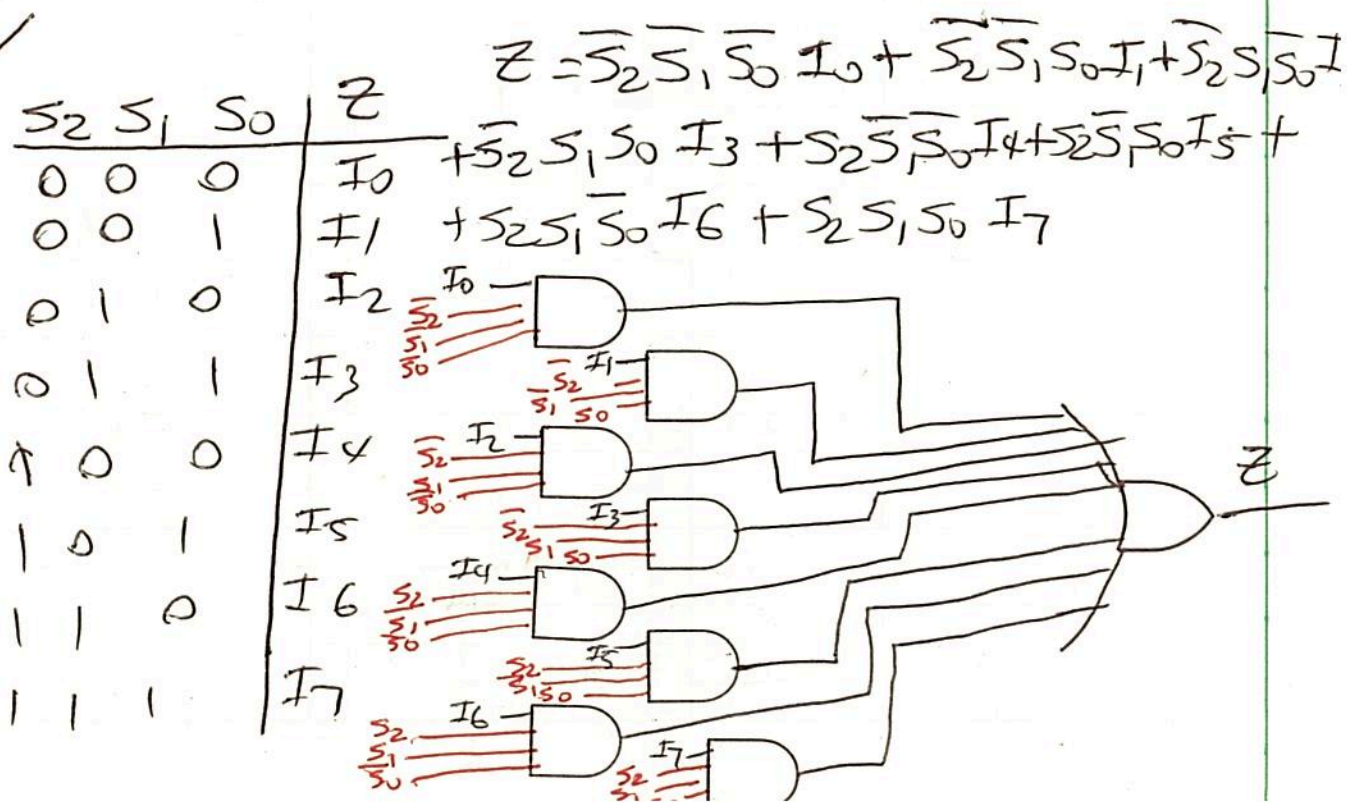
$$F(x, y, z, w) = \sum m(1, 3, 5, 7, 9, 11, 12, 15) + d(2, 4, 10)$$



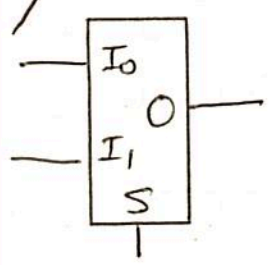
9

D ₁₅	D ₁₄	D ₁₃	D ₁₂	D ₁₁	D ₁₀	D ₉	D ₈	D ₇	D ₆	D ₅	D ₄	D ₃	D ₂	D ₁	D ₀	x	y	z	w	v	
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	x	x	x	x	0
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	0	0	0	0	1	1
0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	x	0	0	0	1	1	1
0	0	0	0	0	0	0	0	0	0	0	0	0	0	1	x	x	0	0	1	0	1
0	0	0	0	0	0	0	0	0	0	0	0	0	1	x	x	x	0	0	1	1	1
0	0	0	0	0	0	0	0	0	0	0	0	1	x	x	x	x	0	1	0	0	1
0	0	0	0	0	0	0	0	0	1	x	x	x	x	x	x	0	1	0	1	1	1
0	0	0	0	0	0	0	1	x	x	x	x	x	x	x	x	0	1	1	1	1	1
0	0	0	0	0	0	1	x	x	x	x	x	x	x	x	x	1	0	0	0	1	1
0	0	0	0	0	1	x	x	x	x	x	x	x	x	x	x	1	0	0	1	1	1
0	0	0	0	1	x	x	x	x	x	x	x	x	x	x	x	1	0	1	1	1	1
0	0	0	1	x	x	x	x	x	x	x	x	x	x	x	x	1	1	0	0	1	1
0	0	1	x	x	x	x	x	x	x	x	x	x	x	x	x	1	1	0	1	1	1
0	1	x	x	x	x	x	x	x	x	x	x	x	x	x	x	1	1	1	0	1	1
1	x	x	x	x	x	x	x	x	x	x	x	x	x	x	x	1	1	1	1	1	1

10

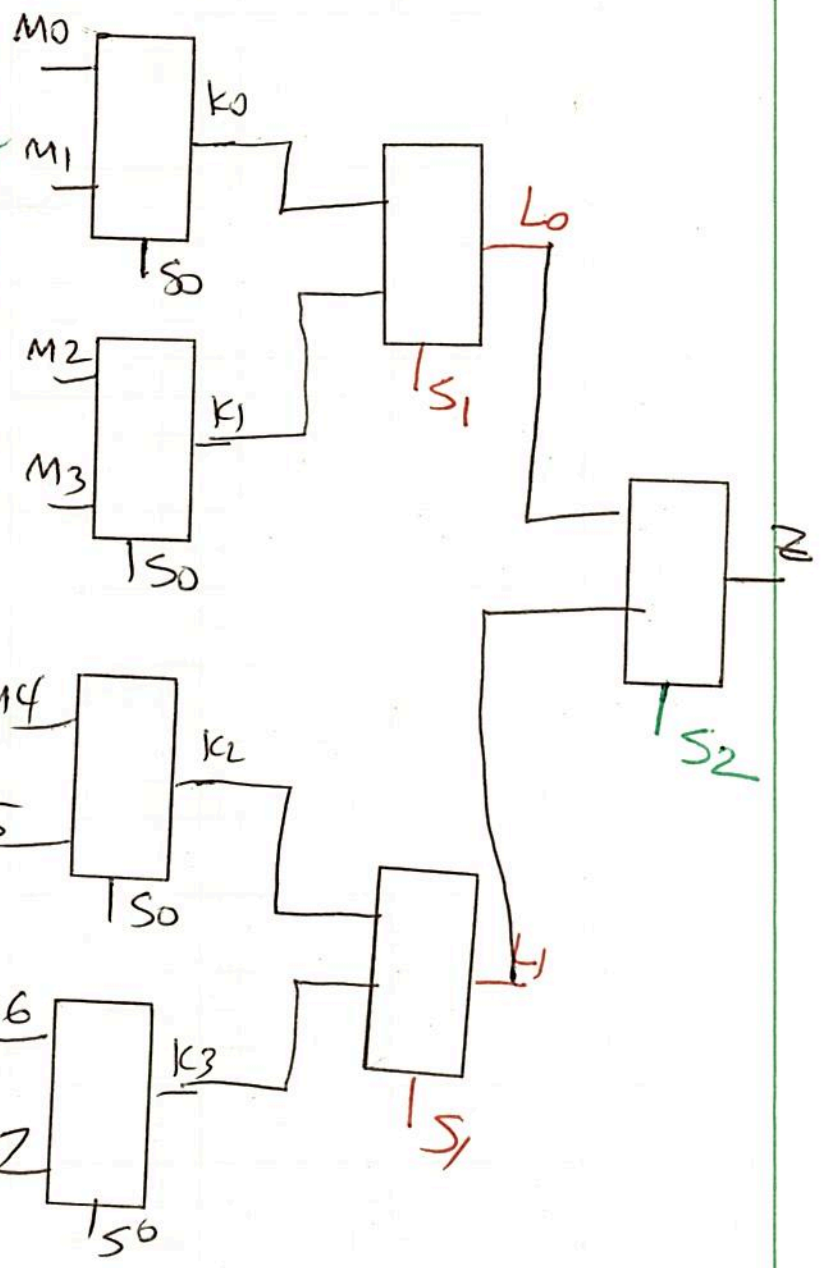


//



S	O
0	I_0
1	I_1

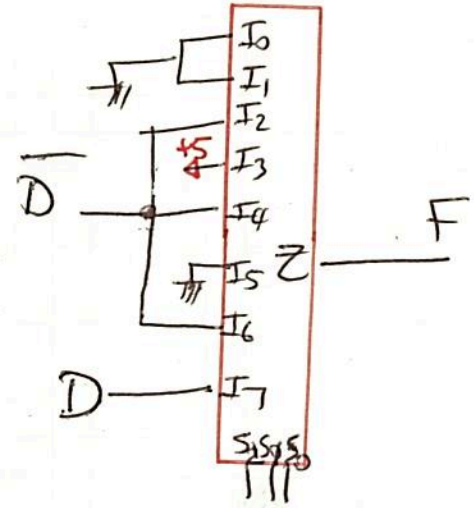
S_2	S_1	S_0	Z
0	0	0	M_0 k_0
0	0	1	M_1
0	1	0	M_2 k_1
0	1	1	M_3
1	0	0	M_4 k_2
1	0	1	M_5
1	1	0	M_6 k_3
1	1	1	M_7



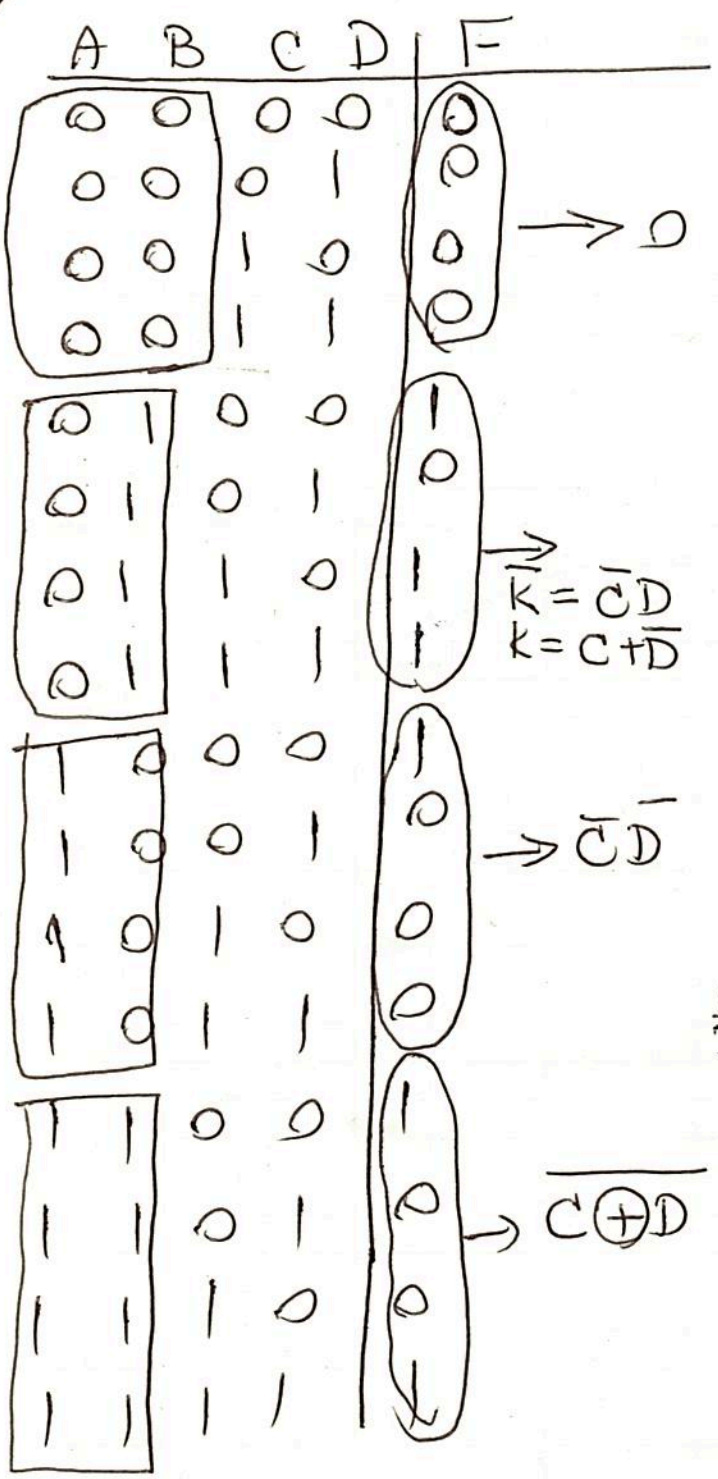
b

A	B	C	D	F
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	1
0	1	0	1	0
0	1	1	0	1
0	1	1	1	0
1	0	0	0	1
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	1

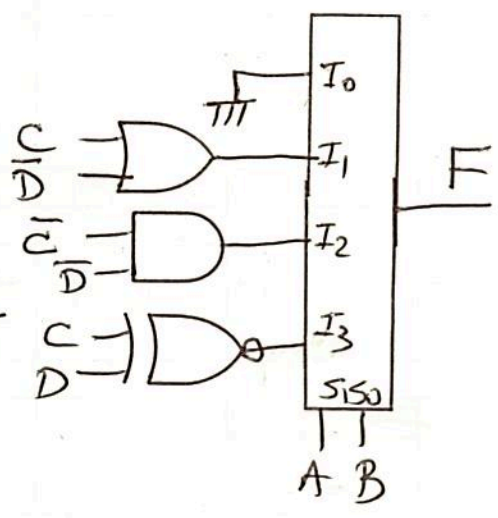
S ₂	S ₁	S ₀	Z
0	0	0	F ₀ = 0
0	0	1	F ₁ = 0
0	1	0	F ₂ = D̄
0	1	1	F ₃ = 1
1	0	0	F ₄ = D̄
1	0	1	F ₅ = 0
1	1	0	F ₆ = D̄
1	1	1	F ₇ = D



B



S_1	S_0	
0	0	$I_0 = 0$
0	1	$I_1 = \overline{C}D$
1	0	$I_2 = C\overline{D}$
1	1	$I_3 = \overline{C \oplus D}$



15 PT.

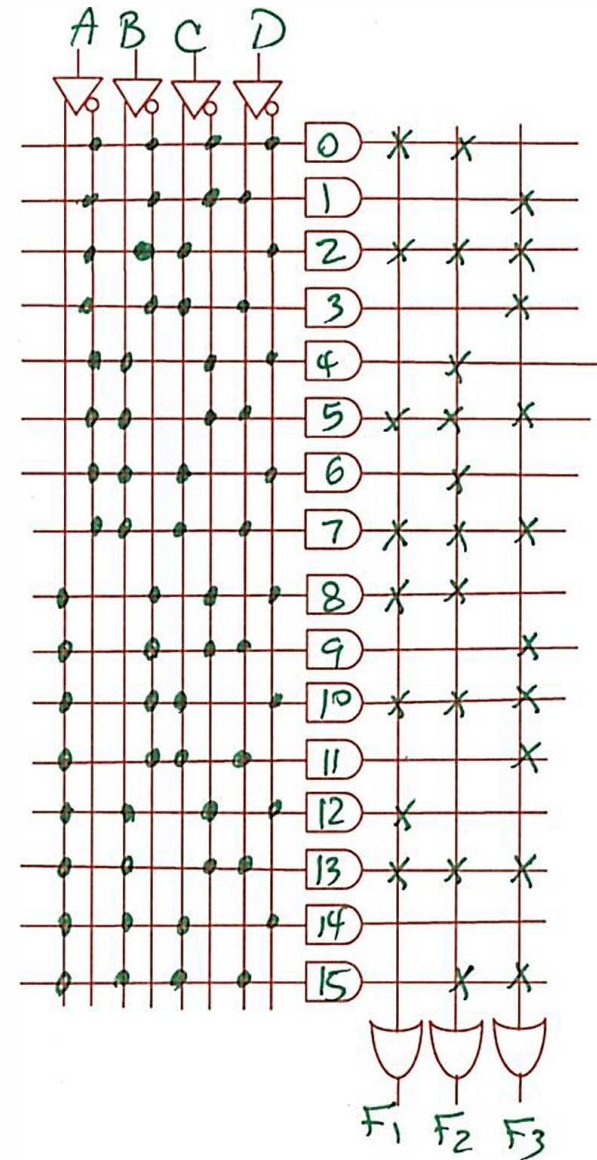
Problem 14

Implement the following functions using a PLE.

$$F_1 = \sum m(0, 2, 5, 7, 8, 10, 12, 13)$$

$$F_2 = \sum m(0, 2, 4, 5, 6, 7, 8, 10, 13, 15)$$

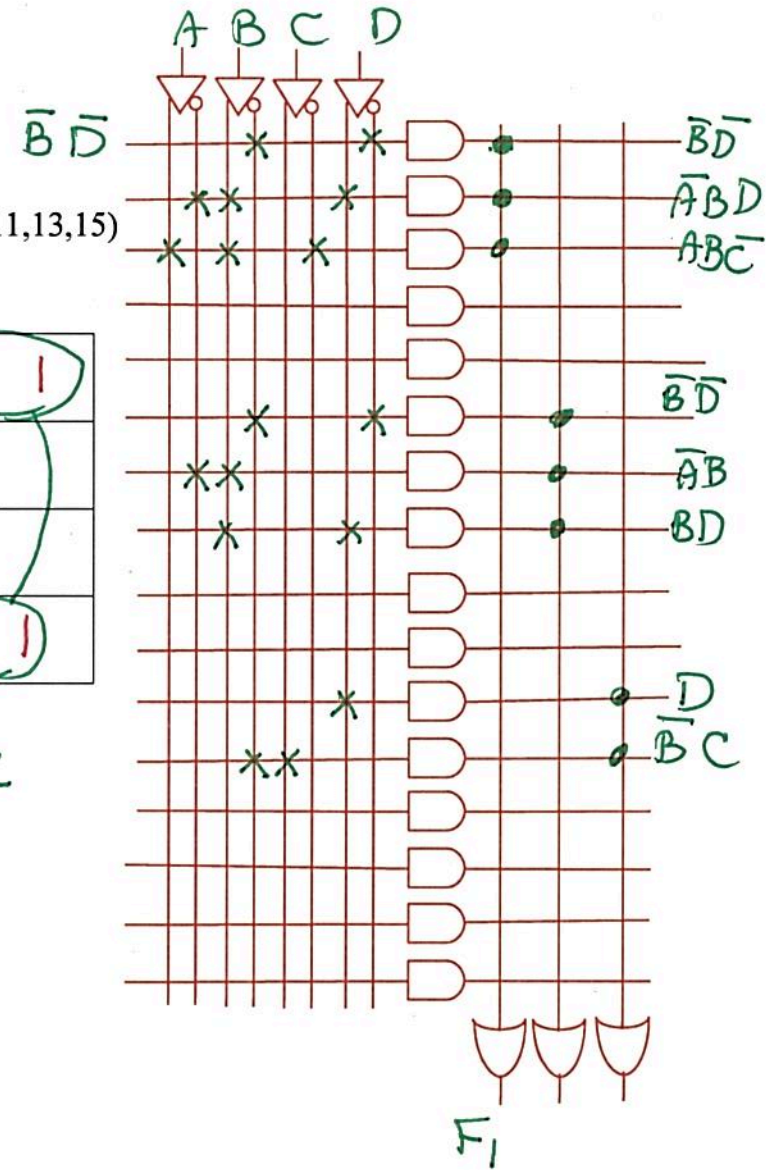
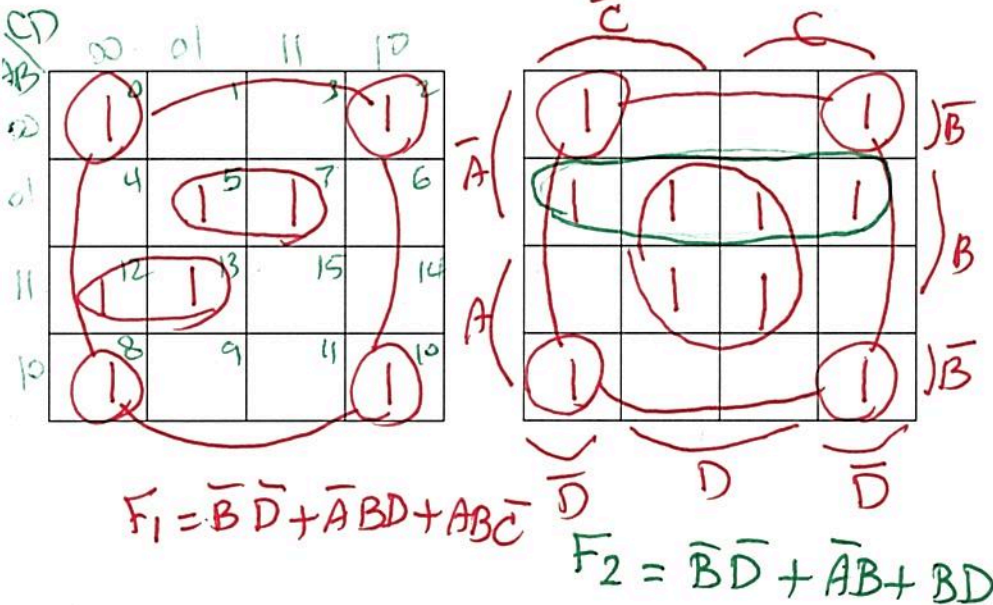
$$F_3 = \sum m(1, 2, 3, 5, 7, 9, 10, 11, 13, 15)$$



Problem 15

Repeat problem 14 for a PAL. (You must simplify your answer)

$$F_1 = \sum m(0, 2, 5, 7, 8, 10, 12, 13) \quad F_2 = \sum m(0, 2, 4, 5, 6, 7, 8, 10, 13, 15) \quad F_3 = \sum m(1, 2, 3, 5, 7, 9, 10, 11, 13, 15)$$



16

Repeat problem 14 for a PLA. (You must simplify your answer)

$$F_1 = \sum m(0, 2, 5, 7, 8, 10, 12, 13) = \overline{B}\overline{D} + \overline{A}BD + ABC\overline{C}$$

$$F_2 = \sum m(0, 2, 4, 5, 6, 7, 8, 10, 13, 15) = \overline{B}\overline{D} + \overline{A}B + BD$$

$$F_3 = \sum m(1, 2, 3, 5, 7, 9, 10, 11, 13, 15) = D + \overline{B}C$$

